Calibrationless OSCAR-based Image Reconstruction in Compressed Sensing Parallel MRI

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ISBI, 2019, Venice, Italy

Outline

- Motivation & Context
 - Why non-Cartesian acquisition
 - Non-Cartesian MR mage reconstruction in parallel imaging
- Calibration-less MR image reconstruction
 - Problem statement
 - Joint sparsity regularization
- Experiments & Results
 - Experimental set-up
 - Results
- Conclusion & Discussion

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Anatomical MRI

Anatomical MRI is generally acquired using Cartesian sampling.

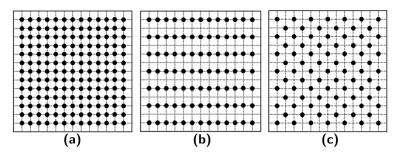


Figure: Typical (a) Cartesian (b) parallel acquisition (c) CAIPIRINHA¹ acquisition

... however in some cases non-Cartesian trajectories are useful ...

¹Breuer et al. 2006, Magnetic Resonance in Medicine.

A non-exhaustive list of usage

- For ultra-short echo time imaging²
- X-nuclei imaging (TPI³)
- To correct for motion, especially for abdominopelvic MRI⁴

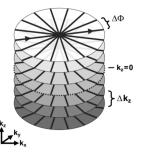


Figure: Stack of stars used for VIBE acquisition

²Johnson et al. 2013, *Magnetic Resonance in Medicine*.

³Boada et al. 1997, Magnetic Resonance in Medicine.

⁴Chandarana et al. 2014, *European radiology*.

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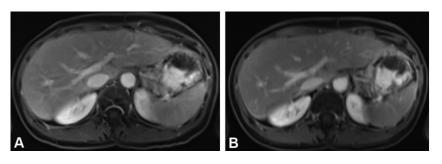


Figure: A: Free-breathing stack-of-stars VIBE, B: Breath-holding conventional VIBE

²Johnson et al. 2013, *Magnetic Resonance in Medicine*.

³Boada et al. 1997, *Magnetic Resonance in Medicine*.

⁴Chandarana et al. 2014, *European radiology*.

Renewed interest to speed-up acquisition in the context of Compressed Sensing⁵.

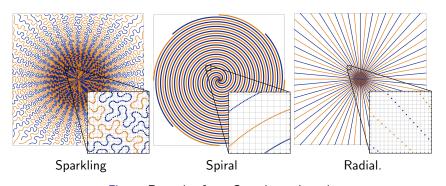


Figure: Example of non-Cartesian trajectories.

⁵Lazarus et al. 2019, *Magnetic Resonance in Medicine*.

Renewed interest to speed-up acquisition in the context of Compressed Sensing⁵.

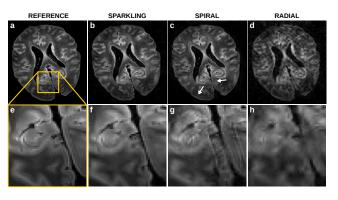


Figure: Comparison of different acquisition trajectories with 16-fold accelerated acquisition on T2*-weighted images.

⁵Lazarus et al. 2019, *Magnetic Resonance in Medicine*.

Parallel imaging acquisition: collect multiple k-space data using a multi-receiver coil as the latter is known to boost the SNR.



Illustration of multi-receiver coil (phased array).

How do we reconstruct MR images from non-Cartesian k-space measurements in parallel imaging?

Self-calibrating methods

Non-Cartesian reconstruction techniques can be split in two categories:

Self-calibrating methods:

⁷Samsonov et al. 2004, Magnetic Resonance in Medicine.

⁸Uecker et al. 2014, Magnetic Resonance in Medicine.

Self-calibrating methods

- Self-calibrating methods:
 - require a region where the signal has been sampled at least at the Nyquist rate

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Self-calibrating methods

- Self-calibrating methods:
 - require a region where the signal has been sampled at least at the Nyquist rate
 - model the coil sensitivity profiles S_ℓ for all channels $\ell=1,\ldots,L^{7,8}$

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⁸Uecker et al. 2014, Magnetic Resonance in Medicine. OSCAR-based p-MRI reconstruction

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OSCAR-based p-MRI reconstruction

solve an inverse problem and recover a single full FOV image:

$$\widehat{\boldsymbol{x}} = \underset{\boldsymbol{x} \in \mathbb{C}^N}{\operatorname{arg min}} \frac{1}{2} \sum_{\ell=1}^{L} \sigma_{\ell}^{-2} \| \boldsymbol{F}_{\Omega} \boldsymbol{S}_{\ell} \boldsymbol{x} - \boldsymbol{y}_{\ell} \|_{2}^{2} + \lambda \| \boldsymbol{\Psi} \boldsymbol{x} \|_{1}$$
 (1)

8 / 29

⁷Samsonov et al. 2004, Magnetic Resonance in Medicine.

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Note: Extraction of coil sensitivity maps is challenging in non-Cartesian case

⁷Samsonov et al. 2004, Magnetic Resonance in Medicine.

⁸Uecker et al. 2014, *Magnetic Resonance in Medicine*. 🔻 🖘 🔻 🔻 🔻 🗦 🔻 🗨 🗨

Calibration-less methods

- Calibration-less methods:
 - do not require any calibration region

⁹Trzasko and Manduca 2011, Signals, Systems and Computers (ASILOMAR), 2011 Conference Record of the Forty Fifth Asilomar Conference on.

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 - do not require any calibration region
 - solve an inverse problem but recover channel-specific images

⁹Trzasko and Manduca 2011, Signals, Systems and Computers (ASILOMAR), 2011 Conference Record of the Forty Fifth Asilomar Conference on.

¹⁰Majumdar and Ward 2012, Magnetic Resonance in Medicine → ⟨♂⟩ ⟨♂⟩ ⟨♂⟩ ⟨०⟩

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 - ullet use the redundant information given by each coil to impose constraints such as low-rank CLEAR 9 or group-sparsity CALM 10

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Calibration-less methods

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 - do not require any calibration region
 - solve an inverse problem but recover channel-specific images
 - use the redundant information given by each coil to impose constraints such as low-rank CLEAR⁹ or group-sparsity CALM¹⁰
 - more likely to be used for on-line image reconstruction

⁹Trzasko and Manduca 2011, Signals, Systems and Computers (ASILOMAR), 2011 Conference Record of the Forty Fifth Asilomar Conference on.

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Problem statement

Calibration-less MR image reconstruction problem solved using an *analysis* formulation:

Definition

MR image reconstruction is formulated as follows:

$$\widehat{\underline{x}} = \underset{\underline{x} \in \mathbb{C}^{N \times L}}{\min} \left\{ \frac{1}{2} \sum_{\ell=1}^{L} \sigma_{\ell}^{-2} \| F_{\Omega} x_{\ell} - y_{\ell} \|_{2}^{2} + g(T\underline{x}) \right\}, \tag{2}$$

with:

- ullet $oldsymbol{y}_{\ell} \in \mathbb{C}^{M}$ the $\ell^{ extstyle extsty$
- $x_\ell \in \mathbb{C}^N$ the $\ell^{ exttt{th}}$ channel-specific reconstructed image (ex. N=512 imes 512)
- ullet F_{Ω} is the forward under-sampling Fourier operator
- ullet $T\in\mathbb{C}^{N_{\Psi} imes N}$ linear operator related to a sparse decomposition
- g is a convex regularization term that promotes sparsity

Optimization algorithm

Primal dual optimization

We aim to find:

$$\underline{\widehat{x}} \in \underset{x \in \mathbb{C}^{N \times L}}{\operatorname{argmin}} [f(\underline{x}) + g(T\underline{x})] \tag{3}$$

where:

- f is convex, differentiable on $\mathbb{C}^{N\times L}$ and its gradient is β -Lipschitz
- $g \in \Gamma_0(\mathbb{C}^{N_\Psi \times L})$ with a closed form proximity operator, given by:

$$\operatorname{prox}_{g}(\underline{z}) = \operatorname*{argmin}_{\boldsymbol{v} \in \mathbb{C}^{N_{\Psi} \times L}} \frac{1}{2} \|\underline{z} - \boldsymbol{v}\|^{2} + g(\boldsymbol{v}) \tag{4}$$

Note: Those are standard assumption in optimization based image reconstruction methods.

Optimization algorithm

Condat-Vũ sequence

Using a primal-dual optimization method proposed by Condat- $V\tilde{u}^{11,12}$:

Algorithm 1: Condat-Vũ algorithm

initialize k= 0, au> 0, $\kappa>$ 0, \underline{x}_{0} , \underline{z}_{0} ;

while $k \leq K$ do

$$\begin{aligned} & \underline{x}_{k+1} \coloneqq \underline{x}_k - \tau \left(\nabla f(\underline{x}_k) + T^* \underline{z}_k \right); \\ & \underline{w}_{k+1} \coloneqq \underline{z}_k + \kappa T \left(2\underline{x}_{k+1} - \underline{x}_k \right); \\ & \underline{z}_{k+1} \coloneqq \underline{w}_{k+1} - \kappa \operatorname{prox}_{g/\kappa} \left(\underline{\underline{w}_{k+1}}_{\kappa} \right); \end{aligned}$$

end

with:

• the algorithm weakly converges to the solution of Eq. (3) if

$$\frac{1}{\tau} - \kappa |||\boldsymbol{T}|||^2 \ge \frac{\beta}{2}$$

ullet au and κ hyper-parameters set as follows: $au:=rac{1}{eta}$, $\kappa:=rac{eta}{2|||T|||^2}$



¹¹Condat 2013, Journal of Optimization Theory and Applications.

¹²Vũ 2013, Advances in Computational Mathematics.

Joint sparsity regularization

Group-LASSO

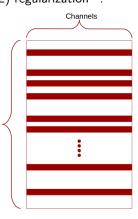
Parallel imaging has been proved to have tighter recovery guarantees than single channel acquisition when combined with Group-LASSO (GL) regularization ¹³.

Definition

The group-LASSO penalty is defined as follows:

$$g_{\mathrm{GL}}(\underline{z}) = \|\underline{z}\|_{1,2} = \sum_{s=1}^{S} \left(\lambda \gamma^{s} \sum_{p=1}^{P_{s}} \sqrt{\sum_{\ell=1}^{L} |z_{sp\ell}|^{2}} \right)$$

- ullet λ and γ are positive hyper-parameters
- s models the scale or subband dependence



Soefficients

 $^{^{13}}$ Chun, Adcock, and Talavage 2016, *IEEE Transactions on Medical Imaging*. For $\gamma=1$ the algorithm corresponds to Majumdar and Ward, *Magnetic Resonance in*

Joint sparsity regularization

Sparse group-LASSO

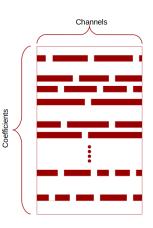
Variant: Sparse group-LASSO¹⁵ (sGL)

Definition

$$\forall \underline{z} \in \mathbb{C}^{N_{\Psi} \times L}, g_{\mathrm{sGL}}(\underline{z}) = g_{\mathrm{GL}}(\underline{z}) + \mu \, \|\underline{z}\|_{1} \qquad (5)$$

ullet μ being positive hyper-parameter.

sGL proximity operator¹⁸ is closed form and corresponds to the composition of GL proximity operator with soft-thresholding.



¹⁵Friedman, Hastie, and Tibshirani 2010, arXiv preprint arXiv:1001.0736.

Joint sparsity regularization

Octagonal Shrinkage and Clustering Algorithm for Regression

Inferring the structure via a pairwise ℓ_{∞} norm. OSCAR regularization¹⁶:

Definition

$$g_{\text{OSCAR}}(z) = \sum_{s=1}^{S} \lambda \left[\sum_{j=1}^{P_s L} |z_{sj}| + \gamma \sum_{j < k} \max\{|z_{sj}|, |z_{sk}|\} \right]$$

$$= \sum_{s=1}^{S} \lambda \left[\sum_{j=1}^{P_s L} (\gamma(j-1) + 1) |z_{sj}| \right]$$
(6)

where:

- $\underline{z}_{\downarrow} \in \mathbb{C}^{N_{\Psi} \times L}$ the wavelet coefficients sorted in decreasing order, i.e.: $\forall s \in \mathbb{N}, |z_{s1}| \leq \cdots \leq |z_{sP_sL}|$.
- ullet λ and γ are some positive hyper-parameters that need to be set



¹⁶Bondell and Reich 2008, Biometrics.

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Experimental set-up

Sequence parameters:

- Ex-vivo baboon brain
- 7T Siemens Scanner GRE
- 1Tx/32Rx Nova coil
- Sparkling trajectory
- $390\mu\text{m}\times390\mu\text{m}$ in plane-resolution
- 3mm slice thickness
- Acceleration factor of 15 in time
- Under-sampling factor of 2.5
- T: Undecimated Bi-Orthogonal 7-9 wavelet transform

Hyper-parameters set using a grid-search procedure.

Cartesian scan 512×512 was acquired and used for reference.

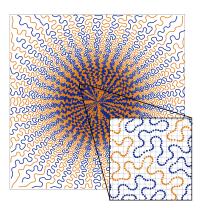


Figure: Sparkling trajectory

Quantitative assessment

Coil combination: Square root of the Sum-Of-Squares Structural SIMilarity Index (SSIM)¹⁷ used to set hyper-parameters

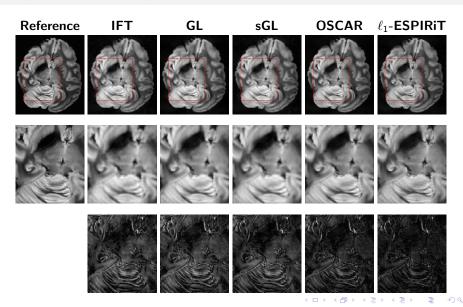
Table: Image quality assessment for all regularizers.

	SSIM	pSNR (dB)	NRMSE
IFT	0.847	26.50	0.263
GL	0.864	26.92	0.254
sGL	0.851	26.77	0.259
OSCAR	0.875	30.49	0.177
ℓ_1 -ESPIRiT	0.874	28.32	0.238

Note: ℓ_1 -ESPIRiT is a self-calibrating method.

¹⁷Wang et al. 2004, *IEEE transactions on image processing*. < □ > < ♠ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > < ₹ > <

Comparison of the Sum-Of-Squares



Quantitative assessment

Comparison between coil images:

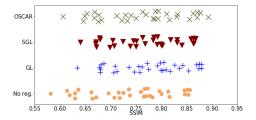


Figure: Assessment of the SSIM score per channel.

Quantitative assessment

Comparison between coil images:

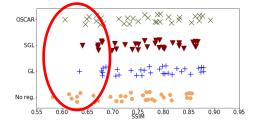
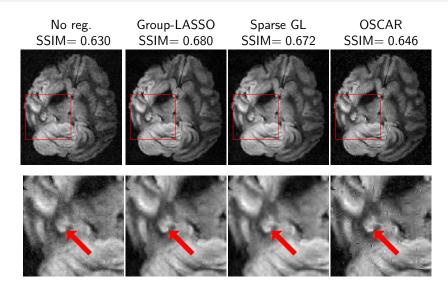


Figure: Assessment of the SSIM score per channel.

Comparison of the image channels: low-SNR channel



Quantitative assessment

Comparison between coil images:

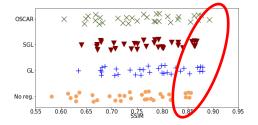
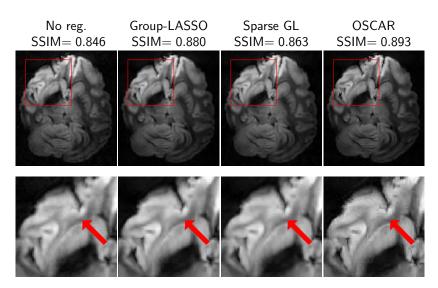


Figure: Assessment of the SSIM score per channel.

Comparison of the image channels: high-SNR channel



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Conclusion & Discussion

Conclusion:

- New parallel CS-MRI reconstruction algorithm
- No sensitivity maps
- OSCAR outperforms group-LASSO and sparse group-LASSO
- ullet OSCAR and ℓ_1 -ESPIRiT are comparable, however the latest is self-calibrating
- Same optimization method to solve calibration-less MR reconstruction

Perspective:

- Extension to 3D-MRI
- Study motion impact on the reconstruction

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